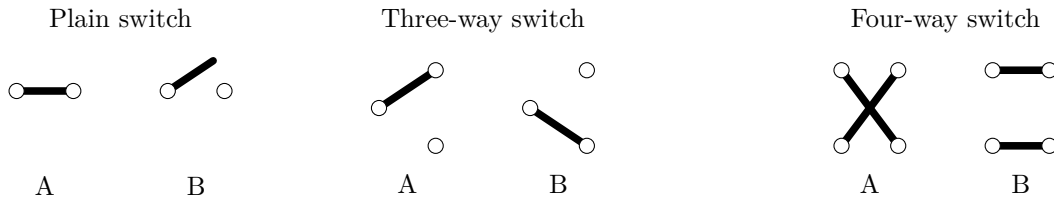


The Electrician's Warm-Up

Prepared by Mark on January 25, 2025

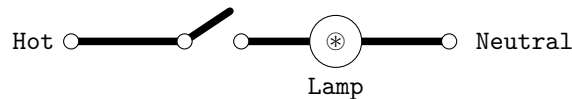
Ivan the electrician is working in an apartment. He has a box of switches, which come in three types:



A switch is always in the “A” or “B” state. Its state changes when you toggle the switch on the wall. Each circle represents a terminal on the switch, and lines represent electrical connections. The two crossing wires in the A state of the four-way switch are **not** connected.

Example 1:

First, Ivan wires a simple light in the kitchen: one switch, one lamp. The result is the following circuit:



Problem 2:

Ivan now needs to wire a hallway. It has two switches, one at each end.

Toggling either switch should toggle the single lamp in the middle.

Which switches should Ivan use, and how should he connect their terminals?

Hint: There are two solutions. One is clever, the other is deadly.

Problem 3:

Next, Ivan goes to the bedroom. There is one switch by the door and one on each side of the bed.

How can he make these three switches control one lamp?

Problem 4: Bonus

Is it possible to do the same with four or more switches? If so, how?